

Errata for the Book

Percy H. Brill, *Level Crossing Methods in Stochastic Models*, Springer, New York, 2008.

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For Additional Information Access

1. <http://web2.uwindsor.ca/math/hlynka/brillbook.html>
2. <http://www.springer.com/math/book/978-0-387-09420-5>

Technical Typos

1. P6,L2. $f_{n+1}(x) = \lambda(P_{n+1}(0) - \lambda P_n(0)B(x)) \rightarrow f_{n+1}(x) = \lambda(P_{n+1}(0) - P_n(0)B(x))$.
2. P11,L11 \uparrow . Subsection 1.4 \rightarrow Subsection 1.5.1.
3. P14,L12. $\lim_{t \rightarrow \infty} \frac{\mathcal{I}(\{0\})}{t} \rightarrow \lim_{t \rightarrow \infty} \frac{\mathcal{I}(\{0\})}{t}$.
4. P14,L3 \uparrow . probability $o(h) \rightarrow$ probability $\lambda h + o(h)$.
5. P14,L1 \uparrow . $\frac{E(\mathcal{D}_t(x+h)) \cdot h \cdot (1-\lambda h) + o(h)}{t}$. The limiting proportion ... $\rightarrow \frac{E(\mathcal{D}_t(x+h)) \cdot h \cdot (1-\lambda h) + o(h)}{t}$. (The numerator $o(h)$ includes the expected time sample path is in $(x, x+h)$ during $(0, t)$ due to sojourns $\neq h$.) The limiting proportion
6. P22,L13 \uparrow of dosing. \rightarrow ... of dosing (Fig. 10.2).
7. P30, Definition 2.4, 3rd line. $X(t_0^-) - \theta d_{t_0}(1-\theta)u_{t_0} \in \mathbf{T} \times \mathbf{A}^c \rightarrow X(t_0^-) - \theta d_{t_0} + (1-\theta)u_{t_0} \in \mathbf{T} \times \mathbf{A}^c$.
8. P49,L2 \uparrow and P50, L1 below Fig. 3.1. $F_{d_1}(0) \rightarrow F_{d_1}^{n-1}(0)$.
9. P51,L1 \uparrow . (Theorem 3.1) \rightarrow (Theorems 3.1, 3.2 below).
10. P53,L4 & L6 below Fig. 3.2, and in the caption of Fig. 3.3. $D_t(x) \rightarrow \mathcal{D}_t(x)$.
11. P53,L4 \uparrow . Theorems 4.1 and 4.1 \rightarrow Theorem 4.1, Section 4.2.1 and Theorem 4.4, Section 4.6.16.
12. P70,L4. $e^{(\mu-\lambda)x} \rightarrow e^{-(\mu-\lambda)x}$.
13. P82,L5. (e.g., [50]) \rightarrow (e.g., [49]). [reference should be [49]]
14. P87, formula (3.90) & one line above it. $e^{(\mu-\lambda)x} \rightarrow e^{-(\mu-\lambda)x}$.
15. P94, formula (3.110), notation. $\mathcal{D}_{d(y)}(x) \rightarrow \mathcal{D}_{d_y}(x)$.
16. P106,L2. $f0) \rightarrow f'(0)$.
17. P116, formula (3.151). $x \in (m, (m+1)D) \rightarrow x \in (mD, (m+1)D)$.
18. P150,L2 of Remark 3.34. $f_1(x)/ \rightarrow f_1(x)$.

19. P156, formula (3.203). $P_0 = \frac{\mu-\lambda}{\mu+e^{-(\mu-\lambda)K}} \rightarrow P_0 = \frac{\mu-\lambda}{\mu-\lambda e^{-(\mu-\lambda)K}}$.
20. P160, formula 3.210. $\sum_{k=1}^{\infty} \rho_1^{k-1} \rightarrow \sum_{k=1}^{\infty} \rho_1^{k-1}$.
21. P164,L2. (Definitions 2.2, 2.3, 2.4, 2.5). \rightarrow (Definitions 2.2, 2.3, 2.4, 2.5 in Subsection 2.4.2).
22. P189,L1 of Proof of Corollary 4.2. In (4.18), (4.19), (4.20) and (4.19), \rightarrow In (4.18), (4.19), (4.20) and (4.21),
23. P220,L6. if it were not blocked. \rightarrow if it were not blocked and cleared.
24. P260,L2. rite \rightarrow right.
25. P270,L5 \uparrow . $\frac{1}{\lim_{t \rightarrow \infty} \mathcal{U}_t(x)} \rightarrow \frac{1}{\lim_{t \rightarrow \infty} \frac{\mathcal{U}_t(x)}{t}}$.
26. P286,L8. $f(x) = Ke^{-\gamma x} \rightarrow f(x) = Ke^{-\gamma x}$.
27. P302,L6 (below Fig. 6.1).
 $W(\tau_n) > y > x > W(\tau_n^-) > 0 \rightarrow W(\tau_n) > y > x > W(\tau_{n+1}^-) > 0$.
28. P306,L3-L4 in (6.12).
L3. $\lambda \int_{z=0}^x \int_{s=t}^{t+h} \overline{B}(x-z) ds dF_{t+s}(z) \rightarrow \lambda \int_{s=t}^{t+h} \int_{z=0}^x \overline{B}(x-z) dF_s(z) ds$;
L4. $\lambda h \int_{z=0}^x \overline{B}(x-z) dF_{t+s^*}(z) \rightarrow \lambda h \int_{z=0}^x \overline{B}(x-z) dF_{s^*}(z)$.
29. P311,L2 above formula (6.23). $\{D_t(x), t \geq 0\} \rightarrow \{\mathcal{D}_t(x), t \geq 0\}$.
Formula (6.24). $E(d_x) \rightarrow E(d_x)$.
30. P312,L1 \uparrow . $F(0) = P_o \rightarrow F(0) = P_0$.
31. P313,L5. as in formula (3.69) \rightarrow as in formula (3.70).
32. P315, (a) L1, Section 6.3.2. $r(0^+)f(0) = P_0 > 0 \rightarrow r(0^+)f(0) = \lambda P_0 > 0$;
(b) RHS of (6.38). $-\frac{r'(x)+\mu-\lambda}{r(x)} \rightarrow -\frac{r'(x)+\mu r(x)-\lambda}{r(x)}$;
(c) RHS of (6.39). $\frac{\lambda P_0}{r(x)} e^{-(\mu-\lambda) \int_{y=0}^x \frac{dy}{r(y)}} \rightarrow \frac{\lambda P_0}{r(x)} e^{-\mu x + \lambda \int_{y=0}^x \frac{dy}{r(y)}}$; also in (6.40).
33. P336,L6 \uparrow and L2 \uparrow . $\overline{B}(y-x) \rightarrow \overline{B}(y-x)$.
34. P337, formula (6.76). Left-most term $r(s)f(x) \rightarrow r(x)f(x)$.
35. P380,L8. $\frac{k}{\lambda} \rightarrow \frac{\lambda}{k}$.
36. P438,L3 \uparrow . as in Theorem 6.2.8, \rightarrow as in Theorem 6.3 in Subsection 6.2.8, .

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